# **Plate With a Hole Optimization - Optimization**

Author: Sebastien Lachance-Barrett, Cornell University

Problem Specification 1. Pre-Analysis & Start-Up 2. Initial Solution 3. Input & Output Parameters 4. Design of Experiments 5. Response Surface 6. Optimization 7. Verification & Validation Exercises Comments

▲ This tutorial was created with an older version of ANSYS (14.5), where the mesh generator and the refinement process was not as strong as it is now. This will result in a different solution than the one shown. (In ANSYS 16.1, the optimization results in a radius of ~1.25in-1.27in and in ANSYS 2019 R2 the optimization results in a radius of ~1.11-1.13 in)

## Optimization

#### Set-Up of Optimization

Begin this step, by double clicking on Optimization.



Response Surface Optimization

At this point, ANSYS must be told that the objective function(volume) is to be minimized while staying below the 32.5 ksi Von Mises stress threshold. First, select "Objectives and Constraints" in the outline window. Then, in the "Table of Schematic B4: Optimization" window, select the parameter to be *P2-Surface Body Volume* and change the objective type to *Minimize*. Next, add in a second parameter which will be *P3-Equivalent (von Mises) Stress Maximum*, change the constraint type to *Values <= Upper Bound* and enter 32500 for the *Upper Bound*. Your table should now look like the one below.

| Table of | Table of Schematic B4: Optimization |  |              |   |                       |             |             |  |  |  |
|----------|-------------------------------------|--|--------------|---|-----------------------|-------------|-------------|--|--|--|
|          | А                                   | В  | С            | D | E                     | F           | G           |  |  |  |
| 1        | Nava                                |  | Objective    | 2 | Constraint            |             |             |  |  |  |
| 2        | INGINE                              | Falanciel                                  | Type Target  |   | Туре                  | Lower Bound | Upper Bound |  |  |  |
| 3        | Minimize P2                         | P2 - Surface Body Volume                   | Minimize 💌   |   | No Constraint         | 1           |             |  |  |  |
| 4        | P3 <= 32500 psi                     | P3 - Equivalent (von-Mises) Stress Maximum | No Objective |   | Values <= Upper Bound | 1           | 32500       |  |  |  |
| *        |                                     | Select a Parameter                         |              |   |                       |             |             |  |  |  |

Now, execute the optimization by clicking on *Update* and click on Optimization from the outline window to view the results. The optimization should yield similar results to the following table.

| Table of Schematic B4: Optimization |   |   |                   |                   |  |  |  |
|-------------------------------------|---|---|-------------------|-------------------|--|--|--|
|                                     | А   | В   | с                 | D                 |  |  |  |
| 1                                   | <ul> <li>Optimization Study</li> </ul>              |   |                   |                   |  |  |  |
| 2                                   | Minimize P2   | Goal, Minimize P2 (Def  | ault importance)  |                   |  |  |  |
| 3                                   | P3 <= 32500 psi                                     | Strict Constraint, P3 values less than or equals to 32500 psi<br>(Default importance) |                   |                   |  |  |  |
| 4                                   | <ul> <li>Optimization Method</li> </ul>             |   |                   |                   |  |  |  |
| 8                                   | Candidate Points                                    |   |                   |                   |  |  |  |
| 9                                   |   | Candidate Point 1   | Candidate Point 2 | Candidate Point 3 |  |  |  |
| 10                                  | P1-DS_R   | 1.5408  | 1.4853            | 1.4298            |  |  |  |
| 11                                  | P2 - Surface Body Volume (in^3)                     | × 9.8136  | <b>XX</b> 9.8267  | <b>XX</b> 9.8395  |  |  |  |
| 12                                  | P3 - Equivalent (von-Mises) Stress<br>Maximum (psi) | 32500   | 32420             | 32342             |  |  |  |

The optimization tool found three candidate points that matched our given constraints and objectives. This computation was pretty fast because the optimization tool used the response surface model (plots) that previously generated. It did not actually solve our model by doing a matrix inversion. Remember that the response surface model is only an approximation of the relationship between the parameters and so our results might not be very accurate. Thankfully, we can solve our model using these candidate points to "verify" that they really do satisfy our constraints.

In the Properties of Schematic B4: Optimization window, insert a check to *Verify Candidate Points* and click on *Update* once again. Notice how much longer it takes to solve our model.

| Propertie | es of Schematic B4: Optimization        |           | - | ņ | × |
|-----------|---|-----------|---|---|---|
|           | A                                       | в         |   |   |   |
| 1         | Property                                | Value     |   |   |   |
| 2         | Design Points                           |           |   |   |   |
| 3         | Preserve Design Points After DX Run     |           |   |   |   |
| 4         | Failed Design Points Management         |           |   |   |   |
| 5         | Number of Retries                       | 0         |   |   |   |
| 6         | <ul> <li>Optimization</li> </ul>        |           |   |   |   |
| 7         | Optimization Method                     | Screening |   |   | ۳ |
| 8         | Number of Samples                       | 1000      |   |   |   |
| 9         | Maximum Number of Candidates            | 3         |   |   |   |
| 10        | Verify Candidate Points                 | <b>V</b>  |   |   |   |
| 11        | <ul> <li>Optimization Status</li> </ul> |           |   |   |   |
| 12        | Number of Evaluations                   | 1002      |   |   |   |
| 13        | Number of Failures                      | 0         |   |   |   |
| 14        | Size of Generated Sample Set            | 1002      |   |   |   |
| 15        | Number of Candidates                    | 3         |   |   |   |

The optimization should yield similar results to the following table. Surprise! Some candidate points do not satisfy the maximum Von Mises stress constraint (now marked with a red cross). This is why it is important to always verify the candidate points.

Note: In version 2019 R2, we found that all three of the candidate points failed at this step, so don't be concerned if that is what you find.

| Table of | Schematic B4: Optimization                          |                       |                                 |                         |                                 |                      |                                 |  |
|----------|---|-----------------------|---------------------------------|-------------------------|---------------------------------|----------------------|---------------------------------|--|
|          | A   | в                     | с                               | D                       | E                               | F                    | G                               |  |
| 1        | Optimization Study                                  |                       |                                 |                         |                                 |                      |                                 |  |
| 2        | Minimize P2 Goal, Minimize P2 (Default importance)  |                       |                                 |                         |                                 |                      |                                 |  |
| 3        | P3 <= 32500 psi                                     | Strict Constraint, P3 | values less than or ea          | quals to 32500 psi (Def | fault importance)               |                      |                                 |  |
| 4        | Optimization Method                                 |                       |                                 |                         |                                 |                      |                                 |  |
| 8        | Candidate Points                                    |                       |                                 |                         |                                 |                      |                                 |  |
| 9        |   | Candidate Point 1     | Candidate Point 1<br>(verified) | Candidate Point 2       | Candidate Point 2<br>(verified) | Candidate Point<br>3 | Candidate Point 3<br>(verified) |  |
| 10       | P1-DS_R   | 1.5                   | 408                             | 1.4                     | 853                             | 1.4298               |                                 |  |
| 11       | P2 - Surface Body Volume (in^3)                     | × 9.8136              | × 9.8136                        | ×× 9.8267               | ×× 9.8267                       | ×× 9.8395            | ×× 9.8395                       |  |
| 12       | P3 - Equivalent (von-Mises) Stress<br>Maximum (psi) | 32500                 | × 32509                         | 32420                   | 32495                           | 32342                | 32345                           |  |

By selecting *candidate points* under the results section of the Outline of Schematic B4: Optimization window, you can also see how the results of each candidate points differ from the results of a specified reference candidate point. Additionally, you can even add new candidate points.

Output parameter values calculated from simulations (design point updates) are displayed in black text, while output parameter values calculated from a response surface are dis- played in blue.

The number of gold stars or red crosses displayed next to each goal-driven parameter indicate how well the parameter meets the stated goal, from three red crosses (the worst) to three gold stars (the best).

Tip: Remember how we specified the radius to range from 1 to 2.5 inches to create the Response Surface? Well we now know that the optimized radius should be around 1.45 inches so no need to have that big of a range anymore. For a second round of optimization (not done in this tutorial), it would be a good idea to go back in Design of Experiments and change the lower and upper bounds to be, say 1.4 and 1.5 inches respectively. A smaller range will give you a more accurate response surface which will help you optimize the radius further.

### **Obtaining Deformation and Stress Results for Selected Design Point**

We will select candidate point 2 as the design point. It is a good idea to review the deformation and stress plots at the chosen design point. To do this, let's set the radius from *Candidate Point 2* as the radius of the hole in *Design Modeler*. Select (*Right Click*) *Candidate Point 2* > *Insert as Design Point*.

| 4 | 0 | Candidate Point 1 (verified) |  |                        | ×                      | 9.8136          | -0.13 % |  |
|---|---|------------------------------|--|------------------------|------------------------|-----------------|---------|--|
| 5 | 0 | Candidate Point 2            |  | 4952                   | xx                     | 9.8267          | 0.00 %  |  |
| 6 | ۲ | Candidate Point 2 (verified) |  | Сору                   |                        |                 |         |  |
| 7 | 0 | Candidate Point 3            |  | Explore Resp           | ponse Surface at Point |                 |         |  |
| 8 | 0 | Candidate Point 3 (verified) |  | Insert as Design Point |                        |                 |         |  |
| - |   |                              |  | Insert as Re           | fineme                 | nt Point        | - H     |  |
| * |   | New Custom Candidate Point   |  | Insert as Ver          | ificatio               | on Point        |         |  |
|   |   |                              |  | Insert as Cu           | stom C                 | Candidate Point |         |  |
|   |   |                              |  | Export Data            |                        |                 |         |  |

Next, click Return to Project and double click on Parameter Set. Selecting Insert as Design Point created the design point DP1. Now in the "Table of Design Points" (Right Click) Current > Duplicate design point.

| Table of Design Points |         |         |    |                                |          |  |  |  |  |
|------------------------|---------|---------|----|--------------------------------|----------|--|--|--|--|
|                        | A       | A B     |    | с                              |          |  |  |  |  |
| 1                      | Name 💌  | P1-DS_R |    | P2 - Surface Body Volume 💌     | P3 - Equ |  |  |  |  |
| 2                      | 2 Units |         |    | in^3                           |          |  |  |  |  |
| 3                      | Current | 2       |    | Copy                           |          |  |  |  |  |
| 4                      | DP 1    | 1.4853  |    | Paste                          |          |  |  |  |  |
| *                      |         |         |    |                                |          |  |  |  |  |
|                        |         |         |    | Set Update Order by Row        |          |  |  |  |  |
|                        |         |         |    | Show Update Order              |          |  |  |  |  |
|                        |         |         |    | Optimize Update Order          |          |  |  |  |  |
|                        |         |         |    | Duplicate Design Point         |          |  |  |  |  |
|                        |         |         |    | Export Design Point as Project |          |  |  |  |  |
|                        |         |         | 73 | Update Selected Design Points  |          |  |  |  |  |
|                        |         |         |    | Copy Design Points to          | •        |  |  |  |  |

You have just duplicated the parameters from the original geometry into the new design point DP2. Now (*Right Click*) DP1 > Copy Inputs to Current and click on Update All Design Points in the toolbar.

| Table of Design Points |         |    |           |                               |       |                         |  |  |  |
|------------------------|---------|----|-----------|-------------------------------|-------|-------------------------|--|--|--|
|                        | А       |    |           | В                             |       | с                       |  |  |  |
| 1                      | Name    | •  | P1-DS_R 💌 |                               | •     | P2 - Surface Body Volum |  |  |  |
| 2                      | Units   | 1  |           |                               |       | in^3                    |  |  |  |
| 3                      | Current | t  | 2         |                               |       | 9.6858                  |  |  |  |
| 4                      | DP 1    |    | -         | 4050                          |       | 14                      |  |  |  |
| 5                      | DP 2    | ٦٩ | 1         | Сору                          |       |                         |  |  |  |
| *                      |         |    |           | Set Upda                      | ate O | rder by Row             |  |  |  |
|                        |         |    |           | Show Update Order             |       |                         |  |  |  |
|                        |         |    |           | Optimize                      | Upd   | ate Order               |  |  |  |
|                        |         | >  | <         | Delete D                      | esign | Point                   |  |  |  |
|                        |         | E  | 2         | Copy inputs to Current        |       |                         |  |  |  |
|                        |         |    | 3         | Duplicate Design Point        |       |                         |  |  |  |
|                        |         |    | 7         | Update Selected Design Points |       |                         |  |  |  |
|                        |         | Ę  | 2         | Copy Design Points to         |       |                         |  |  |  |

The radius of *Candidate point 2* has been inserted as the radius in the *Design Modeler*. Let's now view the results of our model with our optimized radius of 1.4853. Click on *Return to Project* and double click *Results*. The graphs below display the total deformation and the equivalent Von Mises stress. You should realize that we did a fantastic job with this optimization problem! It does not get much better than this as the equivalent Von Mises stress lies just under our constraint. Well...not really. Let's take a look at the verification and validation step.

#### **Total Deformation**



**Equivalent Von Mises Stress** 



Go to Step 7: Verification & Validation

Go to all ANSYS Learning Modules