

# Tensile Bar (Results-Interpretation) - Numerical Results

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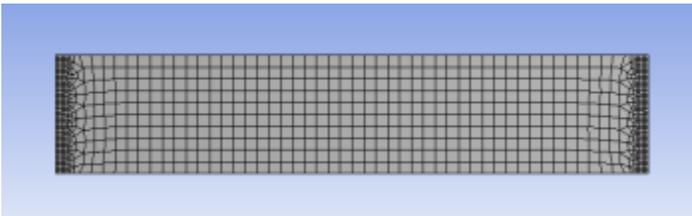
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## Numerical Results

Before we explore the ANSYS results, let's take a peek at the mesh.

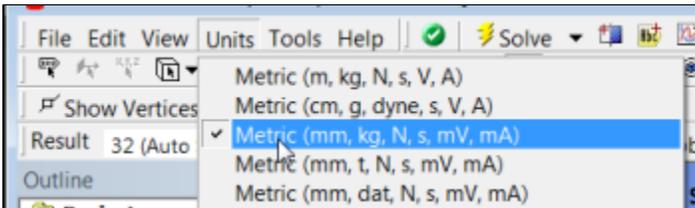
### Mesh

Click on **Mesh** (above **Solution**) in the tree outline. This shows the mesh used to generate the ANSYS solution. The domain is a rectangle. This domain is discretized into a number of small "elements". Recall that ANSYS solves the BVP and calculates the displacements at the nodes. A finer mesh is used near the left and right ends where we expect greater stress concentration. We have checked that the solution presented to you is reasonably independent of the mesh.



### Units

Set the units for the results display by selecting **Units > Metric (mm, kg, N, s, mV, mA)**. The displacements will be reported in *mm* and the stresses in *N/mm<sup>2</sup>* which is equivalent to *MPa*.



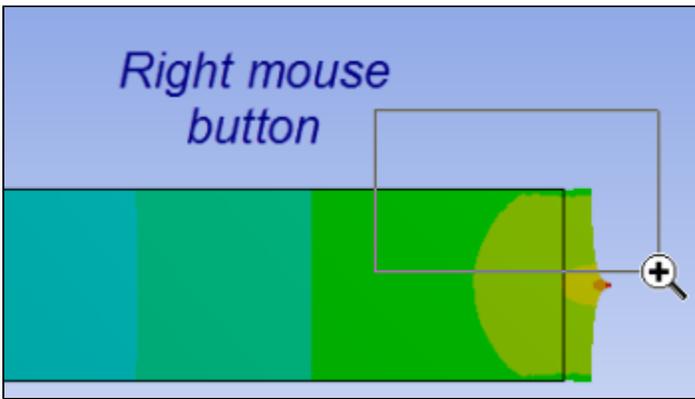
### Displacement

To view the deformed structure, click on **Solution > Displacement** in the tree outline. The black rectangle shows the undeformed structure. The deformed structure is colored by the magnitude of the displacement. The displayed displacement distribution is calculated by interpolating the nodal displacements. Red areas have deformed more and blue areas less. You can see that the left end has not moved as specified in the problem statement. This means this boundary condition has been applied correctly. The displacement increases from left to right as we intuitively expect. There is also not much variation in the *y*-direction. So we can conclude that the model has been constrained properly.

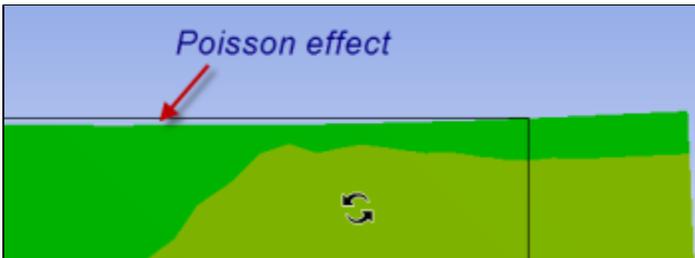
Note the extremely high deformation near the point load. This extremum is unrealistic and should be ignored (there are no point loads in reality).



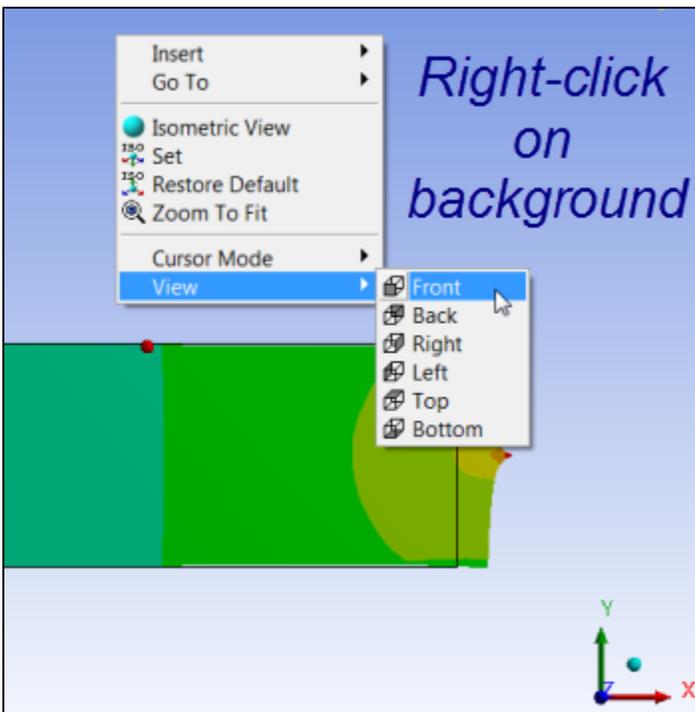
To view the Poisson effect (shrinking in the *y* direction), zoom into the top-right corner by drawing a rectangle around the region with the *right* mouse button.



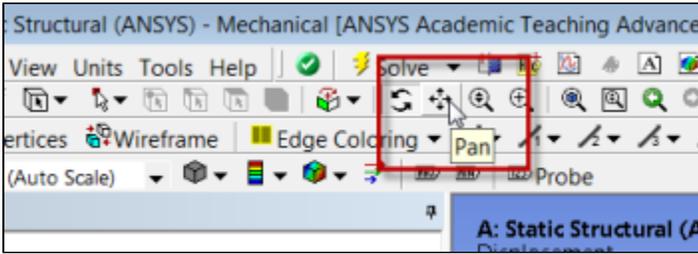
You can do this multiple times to zoom in more. You do indeed see the shrinking in the y-direction as expected but it is small for this model.



You can restore the front view of the entire model by right-clicking in the background and choosing *View > Front*.



Note that you can zoom in and out using the middle mouse wheel. You can translate the model by clicking on the *Pan* button and dragging the model with the left mouse button. There are also a bunch of zoom options next to the *Pan* button.



## sigma\_x

The stresses are derived from the nodal displacements using Hooke's law. In the following video, we look at the  $\sigma_x$  distribution in the interior and at the boundaries and compare the ANSYS values to the values expected from the analytical solution and traction boundary conditions.

Summary of the above video investigating  $\sigma_x$ :

1. Click on probe and hover over the bar. Using the probe may tell you the stress associated with a specific point on the bar.
2. To view the less noticeable stress contours, click on the scale to edit. In this video, the orange (2nd highest value) was changed to 250 and the blue (2nd lowest value) was changed to 50. The contour map changed to display the subtle difference in  $\sigma_x$ .

In the video, we saw that ANSYS's values for  $\sigma_x$  matches with:

- The analytical solution in the interior (away from the left and right boundaries)
  - Traction boundary condition for  $\sigma_x$  at the right boundary
- Note that  $\sigma_x$  at the location of the point load is infinite. So as the mesh is refined further,  $\sigma_x$  at the point load will get larger and larger without bound.

## sigma\_y

Next, let's take a look at  $\sigma_y$ . Click on **Solution > sigma\_y** in the tree outline. Again, probe values in the middle as well as at the ends. Check that:

- The value away from the boundaries is close to zero as expected from the analytical solution. It is not exactly zero because of round-off errors.
- The value at the top and bottom boundaries are close to zero. This agrees with the boundary condition at these boundaries since the traction has to be zero at these free boundaries. In other words, the normal component of the traction acting on these surfaces is  $\sigma_y$  and that has to be zero since the traction on these free surfaces is zero.
- There is significant deviation from the analytical solution at both ends. The analytical solution breaks down at these ends because of the additional assumptions that we made. Note that there are areas where  $\sigma_y$  is negative i.e. compressive.



## tau\_xy

We expect  $\tau_{xy}$  to be zero away from the ends. Near the ends, since  $\sigma_x$  and  $\sigma_y$  are non-zero, we expect

$$\tau_{xy} = \tau_{xy}(x, y)$$

Plot  $\tau_{xy}$ , look at the range of values and use Probe to check actual values. Are the above statements valid?



## Equivalent Stress (Von Mises):

The Equivalent or Von Mises stress is used to predict yielding of the material. We can see that the analytical solution under-predicts the maximum equivalent stress. Thus, one would need to use a large factor of safety if using the analytical result while designing such a structure. One would use a factor of safety with the FEA result also but it does not have to be as large.



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