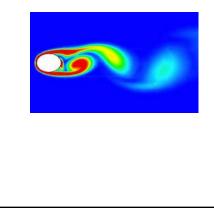
External and Internal Flows

External Flows:

- Flow around a body
- Boundary layer develops freely without constraints from the geometry

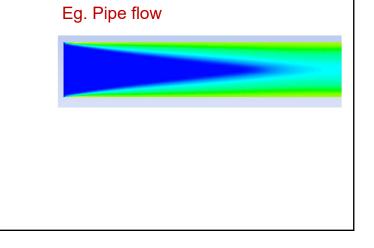
Eg. Cylinder flow

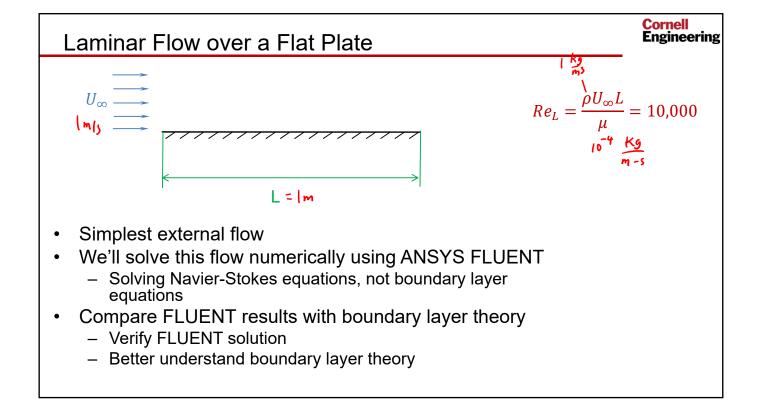


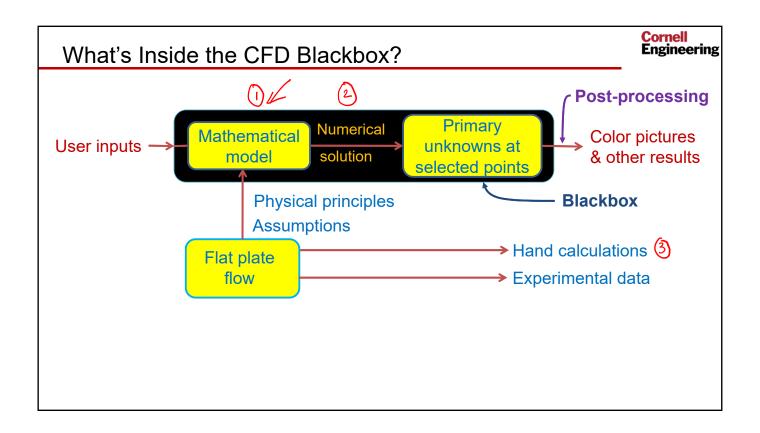
Internal Flows:

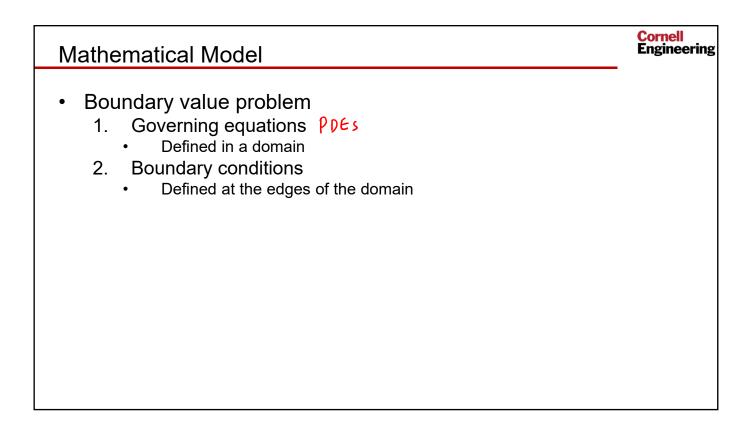
- Flow inside a body
- Boundary layer is unable to develop without eventually being constrained

Cornell Engineering









Governing Equations

• Continuity > $\frac{\partial u}{\partial u} + \frac{\partial v}{\partial u} = 0$

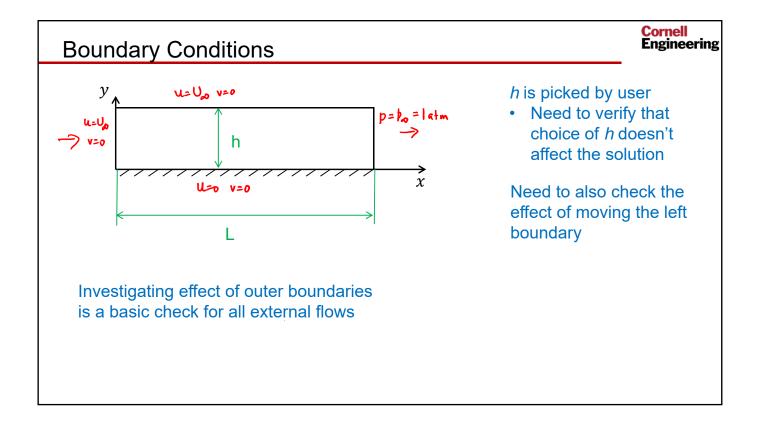
•
$$\vec{F} = m \vec{a}$$
 applied to a vanishingly small chunk of fluid

$$\rho \left(u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} \right) = -\frac{\partial p}{\partial x} + \mu \left(\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} \right)$$

$$\rho \left(u \frac{\partial v}{\partial x} + v \frac{\partial v}{\partial y} \right) = -\frac{\partial p}{\partial y} + \mu \left(\frac{\partial^2 v}{\partial x^2} + \frac{\partial^2 v}{\partial y^2} \right)$$

Assumptions: 20, steady, incompressible, laminar, Newtonian

For an intuitive derivation of these eqs., see https://bit.ly/2UCGThJ

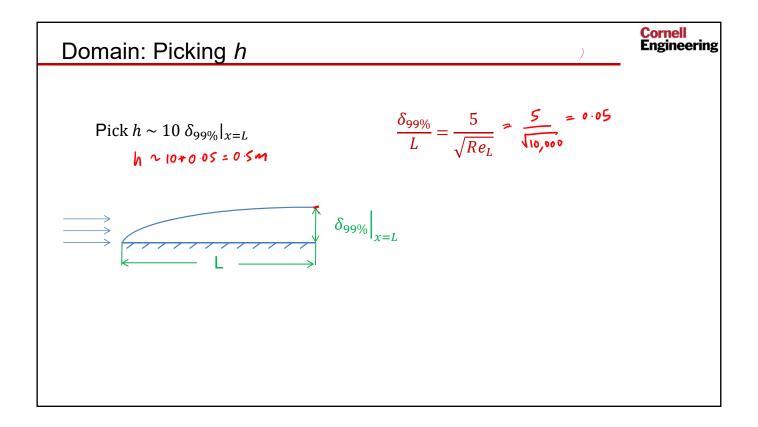


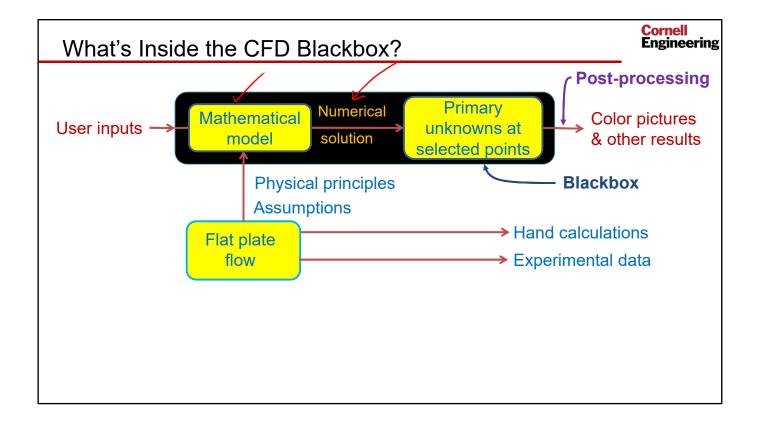
Cornell Engineering

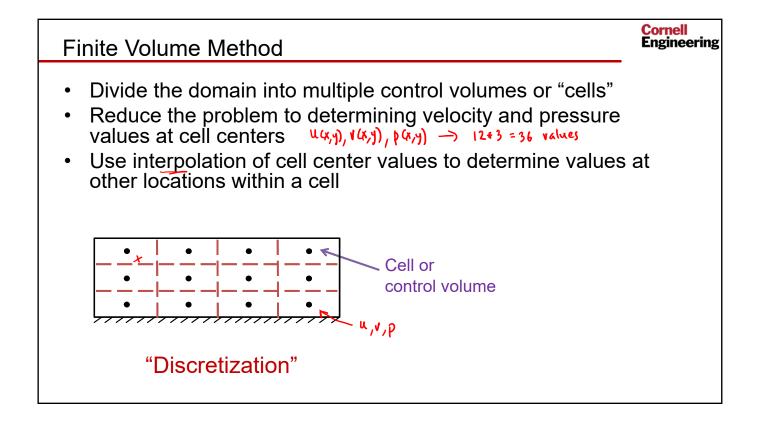
Unknowns: $(x_{3}), (x_{3}), P^{(x_{3})})$

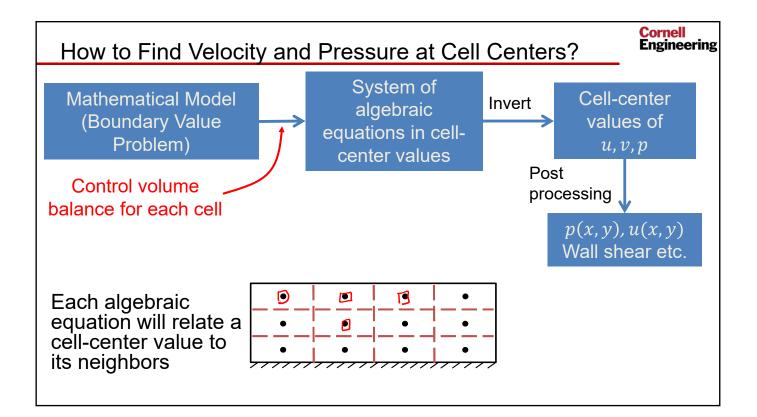
٧y

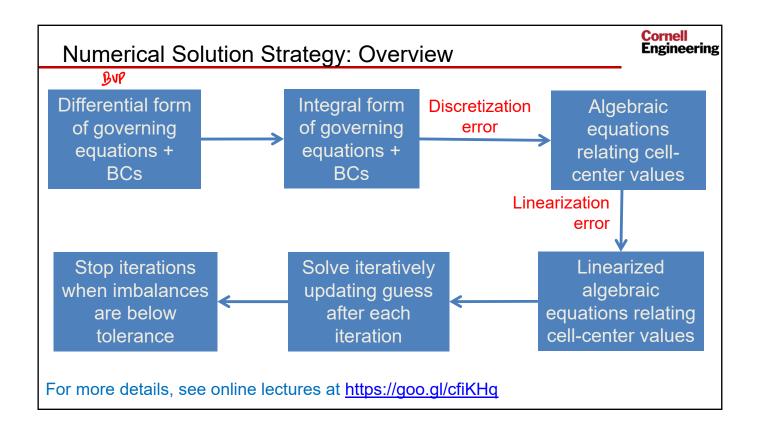
N_x

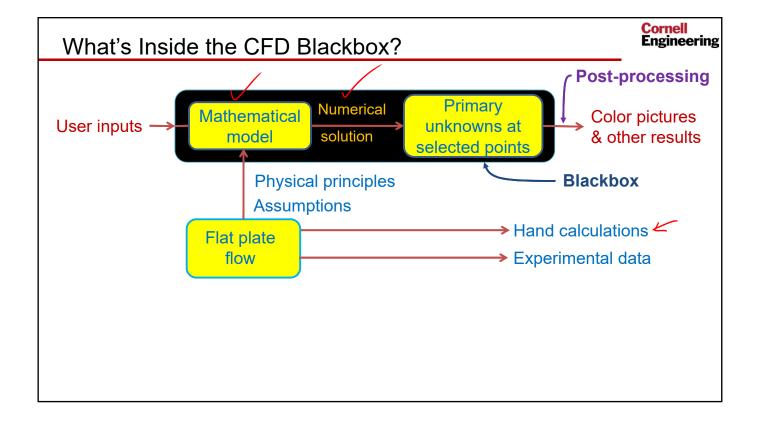


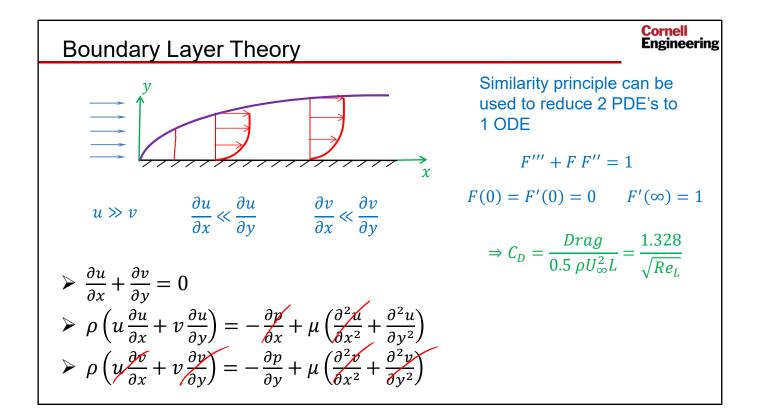


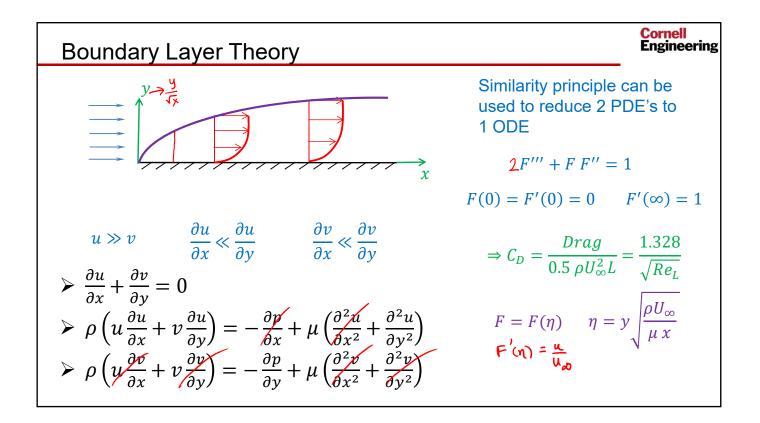


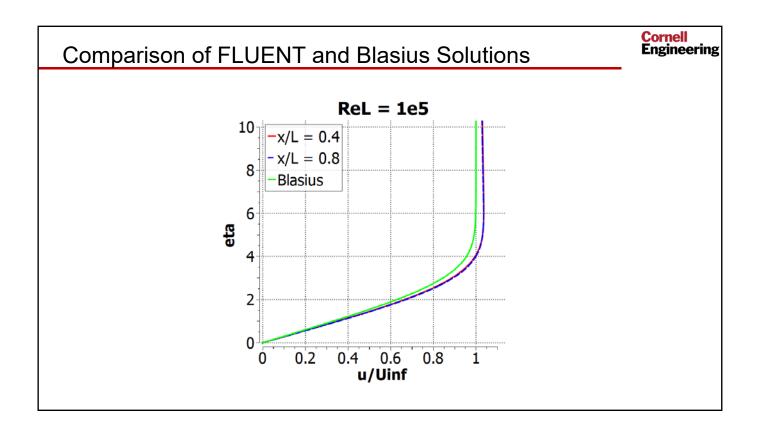


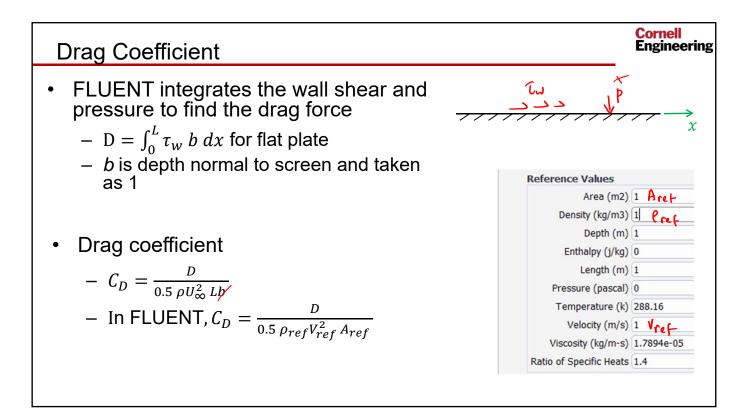


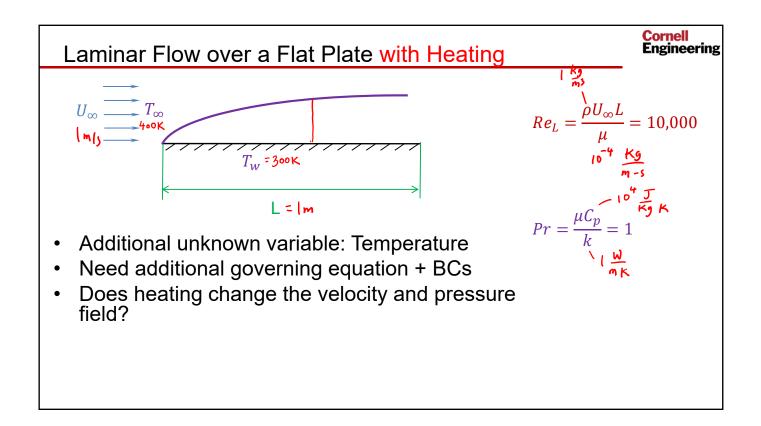












Governing Equations	Cornell Engineering
 Continuity ∂u/∂x + ∂v/∂y = 0 F = m a applied to a vanishingly small chunk of fluid ρ (u ∂u/∂x + v ∂u/∂y) = -∂p/∂x + μ (∂²u/∂x² + ∂²u/∂y²) ρ (u ∂v/∂x + v ∂v/∂y) = -∂p/∂y + μ (∂²v/∂x² + ∂²v/∂y²) Conservation of energy ρC_p(V · V)T = k V²T + (V · V)p + Φ 	Assumptions: 2D, steady, incompressible, laminar, Newtonian Constant properties
Unknowns: $u(x, y), v(x, y), p(x, y), \tau_{x,y}$	
Energy equation is uncoupled	

